#### Big Bang Designing a Statically Typed Scripting Language

#### Pottayil Harisanker Menon, <u>Zachary Palmer</u>, Scott F. Smith, Alexander Rozenshteyn

The Johns Hopkins University

June 11, 2012

(中) (문) (문) (문) (문)

#### Scripting Languages

# ✓ Terse ✓ Flexible ✓ Easy to learn ✓ Amenable to rapid development

## Scripting Languages

# ✓ Terse ✓ Flexible ✓ Easy to learn ✓ Amenable to rapid development ✓ Dynamically typed

## Advantages of Static Typing

▲ロト ▲帰ト ▲ヨト ▲ヨト - ヨ - の々ぐ

- Performance
- Debugging
- Programmer understanding

• e.g. DRuby, Typed Racket



- e.g. DRuby, Typed Racket
- Existing language features are hard to type

- e.g. DRuby, Typed Racket
- Existing language features are hard to type
  - DRuby does not typecheck the entire Ruby API

- e.g. DRuby, Typed Racket
- Existing language features are hard to type
  - DRuby does not typecheck the entire Ruby API
  - Typechecking runtime metaprogramming is hard

- e.g. DRuby, Typed Racket
- Existing language features are hard to type
  - DRuby does not typecheck the entire Ruby API
  - Typechecking runtime metaprogramming is hard

• These systems require programmer annotation

- e.g. DRuby, Typed Racket
- Existing language features are hard to type
  - DRuby does not typecheck the entire Ruby API
  - Typechecking runtime metaprogramming is hard

- These systems require programmer annotation
  - Type annotations reduce terseness

- e.g. DRuby, Typed Racket
- Existing language features are hard to type
  - DRuby does not typecheck the entire Ruby API
  - Typechecking runtime metaprogramming is hard

- These systems require programmer annotation
  - Type annotations reduce terseness
  - Annotations can be overly restrictive

# Let's try designing a typed scripting language **from scratch**

▲ロト ▲帰ト ▲ヨト ▲ヨト - ヨ - の々ぐ

• Design type system and execution model concurrently

- Design type system and execution model concurrently
- Be minimalistic: most features are encoded

- Design type system and execution model concurrently
- Be minimalistic: most features are encoded

• Use static near-equivalents for dynamic patterns

- Design type system and execution model concurrently
- Be minimalistic: most features are encoded

- Use static near-equivalents for dynamic patterns
- Infer all types: no type declarations

- Design type system and execution model concurrently
- Be minimalistic: most features are encoded
- Use static near-equivalents for dynamic patterns
- Infer all types: no type declarations
- Use a whole-program typechecking model

- Design type system and execution model concurrently
- Be minimalistic: most features are encoded
- Use static near-equivalents for dynamic patterns
- Infer all types: no type declarations
- Use a whole-program typechecking model
- Use type information to improve runtime memory layout

# BigBang by Example

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 の�?

◆□ > ◆□ > ◆豆 > ◆豆 > ̄豆 = のへで

• BigBang encodes to a core language

- BigBang encodes to a core language
- TinyBang has very few features:

- BigBang encodes to a core language
- TinyBang has very few features:
  - Primitives

- BigBang encodes to a core language
- TinyBang has very few features:
  - Primitives
  - Labels

- BigBang encodes to a core language
- TinyBang has very few features:
  - Primitives
  - Labels
  - Onions

- BigBang encodes to a core language
- TinyBang has very few features:
  - Primitives
  - Labels
  - Onions
  - Scapes

- BigBang encodes to a core language
- TinyBang has very few features:
  - Primitives
  - Labels
  - Onions
  - Scapes
  - Exceptions

- BigBang encodes to a core language
- TinyBang has very few features:
  - Primitives
  - Labels
  - Onions
  - Scapes
  - Exceptions (and that's all)

• Labels simply wrap data

#### 'name "Tom"

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 の�?

• Labels simply wrap data (polymorphic variants)

- Labels simply wrap data (polymorphic variants)
- Onions combine data

#### 'name "Tom" & 'age 10

▲□▶ ▲圖▶ ★ 国▶ ★ 国▶ - 国 - のへで

- Labels simply wrap data (polymorphic variants)
- Onions combine data
- Data may be unlabeled (vs. extensible records)

#### **'name** "Tom" & **'age** 10 & 3

- Labels simply wrap data (polymorphic variants)
- Onions combine data
- Data may be unlabeled (vs. extensible records)
- Onion data is projected by type

#### (1 & () ) + 2 $\implies$ 3

- Labels simply wrap data (polymorphic variants)
- Onions combine data
- Data may be unlabeled (vs. extensible records)
- Onion data is projected by type
- Onioning is asymmetric (right-precedence)

#### $(1 \& 4) + 2 \implies 6$

- Labels simply wrap data (polymorphic variants)
- Onions combine data
- Data may be unlabeled (vs. extensible records)
- Onion data is projected by type
- Onioning is asymmetric (right-precedence)
  - Used to encode overriding

$$(1 \& 4) + 2 \implies 6$$

- Labels simply wrap data (polymorphic variants)
- Onions combine data
- Data may be unlabeled (vs. extensible records)
- Onion data is projected by type
- Onioning is asymmetric (right-precedence)
  - Used to encode overriding
  - Important for type checking (later)

$$(1 \& 4) + 2 \implies 6$$



• Scapes are functions

х -> х

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 の�?

Scapes

• Scapes are functions with input patterns

#### **'A** x & **'B** y -> x + y

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 の�?

Scapes

• Scapes are functions with input patterns

$$(`A x \& `B y \rightarrow x + y) (`A 1 \& `B 2) \\ \implies 3$$

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 の�?

Scapes

- Scapes are functions with input patterns
- Onions of scapes apply the first matching scape

4

Scapes

- Scapes are functions with input patterns
- Onions of scapes apply the first matching scape
- Encodes typecasing

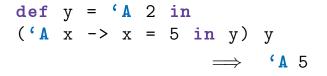
Scapes

- Scapes are functions with input patterns
- Onions of scapes apply the first matching scape
- Encodes typecasing
- Refines First-Class Cases [Chae et al. '06]

#### **Mutation**

▲□▶ ▲圖▶ ★ 国▶ ★ 国▶ - 国 - のへで

#### • Label contents are mutable



#### **Mutation**

- Label contents are mutable
- But onioning is functional extension

def x = 'A 0 & 'B 1 in
def y = 'B 2 & 'C 3 in
def z = x & y in
x

#### ⇒ **'A** 0 & **'B** 1

#### **Mutation**

- Label contents are mutable
- But onioning is functional extension

def x = 'A 0 & 'B 1 in
def y = 'B 2 & 'C 3 in
def z = x & y in
z

 $\implies$  **'A** 0 & **'B** 2 & **'C** 3

## Expressiveness

Function self-awareness can be encoded by:

• Adding a 'self match to each pattern

$$x \rightarrow x$$
  
 $\downarrow$   
 $x:$  'self self  $\rightarrow x$ 

▲□▶ ▲圖▶ ★ 国▶ ★ 国▶ - 国 - のへで

Function self-awareness can be encoded by:

• Adding a 'self match to each pattern

Function self-awareness can be encoded by:

- Adding a 'self match to each pattern
- Adding a 'self value to each invocation

**def** factorial = x: int -> if x == 0 then 1 else **self** (x-1) \* x in self 5  $\downarrow$ def factorial = x: int & 'self self -> if x == 0 then 1 else **self** (x-1) \* x in factorial (5 & 'self factorial)

▲□▶ ▲圖▶ ★ 国▶ ★ 国▶ - 国 - のへで

• Objects are encoded as onions

```
class Point {
    int x = 2;
    int y = 3;
    int l1() {
        return x+y;
    }
}
```

- Objects are encoded as onions
- Each field is a labeled value

- Objects are encoded as onions
- Each field is a labeled value
- Message handler scapes encode methods

- Objects are encoded as onions
- Each field is a labeled value
- Message handler scapes encode methods

 $(\mathbf{x} \times \mathbf{x} \rightarrow \mathbf{x}) \circ \cong \mathbf{o} \cdot \mathbf{x}$ 

o ( '11 () &  $\cong$  o.l1() 'self o )

▲ロト ▲母 ト ▲目 ト ▲目 ト ● ○ ○ ○ ○ ○

#### **Encoding Mixins**

Inheritance occurs by onion extension

def mypoint = 'x 2 & 'y 3 &
 ('l1 () -> self.x + self.y)
in def mixinFar =
 ('isFar () -> self.l1() > 26)
in def myFpoint = mypoint & mixinFar
in myFpoint.isFar()

#### **Encoding Mixins**

- Inheritance occurs by onion extension
- Mixins are the extension onion

def mypoint = 'x 2 & 'y 3 &
 ('l1 () -> self.x + self.y)
in def mixinFar =
 ('isFar () -> self.l1() > 26)
in def myFpoint = mypoint & mixinFar
in myFpoint.isFar()

◆□▶ ◆□▶ ◆三▶ ◆三▶ ◆□▶ ◆□

#### **Encoding Classes**

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 の�?

• Classes are object factories

#### **Encoding Classes**

- Classes are object factories
- Subclass factories instantiate and extend

#### **Encoding Overloading**

• Overloading is trivial with scapes

◆□▶ ◆□▶ ◆三▶ ◆三▶ ◆□▶ ◆□

#### **Encoding Overloading**

- Overloading is trivial with scapes
- Onion extension allows incremental overloading

#### **Encoding Overloading**

- Overloading is trivial with scapes
- Onion extension allows incremental overloading

• Default arguments are easy too

• BigBang uses TinyBang as a core language

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 の�?

• BigBang uses TinyBang as a core language

 BigBang will provide macros for syntax/features

- BigBang uses TinyBang as a core language
- BigBang will provide macros for syntax/features
- self, class syntax, etc. defined in this way

- BigBang uses TinyBang as a core language
- BigBang will provide macros for syntax/features
- self, class syntax, etc. defined in this way

• User extensions can be specified

- BigBang uses TinyBang as a core language
- BigBang will provide macros for syntax/features
- self, class syntax, etc. defined in this way
- User extensions can be specified
- Similar to Racket (Languages as Libraries [Tobin-Hochstadt et al., 2011])

・ロト ・ 日 ・ モ ト ・ モ ・ うへぐ

# Typing

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへぐ

A scripting language's type system must be: **★** Expressive

▲ロト ▲帰ト ▲ヨト ▲ヨト 三日 - の々ぐ

#### A scripting language's type system must be: ★ Expressive

• Duck typing, conditional types

- A scripting language's type system must be: ★ Expressive
  - Duck typing, conditional types
  - No arbitrary cutoffs

- A scripting language's type system must be: ★ Expressive
  - Duck typing, conditional types
  - No arbitrary cutoffs

✦ Comprehensible

- A scripting language's type system must be: ★ Expressive
  - Duck typing, conditional types
    - No arbitrary cutoffs
  - Comprehensible
    - Types should be legible

- A scripting language's type system must be:
  - ★ Expressive
    - Duck typing, conditional types
    - No arbitrary cutoffs
  - Comprehensible
    - Types should be legible
    - Sources of type errors must be clear

- A scripting language's type system must be:
  - ★ Expressive
    - Duck typing, conditional types
    - No arbitrary cutoffs
  - Comprehensible
    - Types should be legible
    - Sources of type errors must be clear

• Intuitive non-local inference

- A scripting language's type system must be:
  - ★ Expressive
    - Duck typing, conditional types
    - No arbitrary cutoffs
  - Comprehensible
    - Types should be legible
    - Sources of type errors must be clear

• Intuitive non-local inference

# Efficient

- A scripting language's type system must be:
  - ★ Expressive
    - Duck typing, conditional types
    - No arbitrary cutoffs
  - Comprehensible
    - Types should be legible
    - Sources of type errors must be clear
    - Intuitive non-local inference
  - # Efficient
    - Short compile times for dev. iterations

- A scripting language's type system must be:
  - ★ Expressive
    - Duck typing, conditional types
    - No arbitrary cutoffs
  - Comprehensible
    - Types should be legible
    - Sources of type errors must be clear
    - Intuitive non-local inference
  - # Efficient
    - Short compile times for dev. iterations

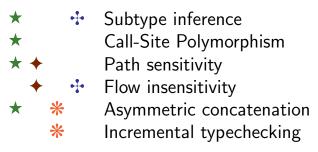
Easy to Use

#### A scripting language's type system must be:

- ★ Expressive
  - Duck typing, conditional types
  - No arbitrary cutoffs
- Comprehensible
  - Types should be legible
  - Sources of type errors must be clear
  - Intuitive non-local inference
- # Efficient
  - Short compile times for dev. iterations
- ✤ Easy to Use
  - Usable to teach introductory courses

# Typing BigBang

For BigBang, we choose:



### $\star$ $\cdot$ Subtype Inference $\cdot$

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへぐ

• No programmer type declarations

## ★ 🕂 Subtype Inference 🕂 ★

▲□▶ ▲□▶ ▲三▶ ▲三▶ 三三 のへで

- No programmer type declarations
- Supports duck-typing

# ★ 🕂 Subtype Inference 🕂 ★

- No programmer type declarations
- Supports duck-typing
- Supports nominal typing (labels as names)

# ★ 🕂 Subtype Inference 🕂 ★

- No programmer type declarations
- Supports duck-typing
- Supports nominal typing (labels as names) (e.g. 'x 1 & 'y 2 & 'Point ())

• All functions polymorphic; no let restriction

- All functions polymorphic; no let restriction
- New contour for each non-recursive call site

- All functions polymorphic; no **let** restriction
- New contour for each non-recursive call site

• Only one contour for each recursive cycle

- All functions polymorphic; no **let** restriction
- New contour for each non-recursive call site

- Only one contour for each recursive cycle
- A variant of both *n*CFA and CPA

▲□▶ ▲圖▶ ▲臣▶ ▲臣▶ ―臣 … のへで

```
def f = x -> 'A x in
def x = f 0 in
def y = f () in
def z = f ('B 2 & 'C 3) in
```

. . .

def f = x -> 'A x in  
def x = f 0 in  
def y = f () in  
def z = f ('B 2 & 'C 3) in  
...  
x 
$$\Longrightarrow$$
 'A 0  
y  $\Longrightarrow$  'A ()  
z  $\Longrightarrow$  'A ('B 2 & 'C 3)

◆□ > ◆□ > ◆ Ξ > ◆ Ξ > Ξ のへで



• Scape application based on pattern match





- Scape application based on pattern match
- · Constraints expanded only if input matches

### ★ + Path Sensitivity + ★

- Scape application based on pattern match
- · Constraints expanded only if input matches

• With polymorphism, gives path sensitivity

### ★ + Path Sensitivity + ★

- Scape application based on pattern match
- Constraints expanded only if input matches
- With polymorphism, gives path sensitivity
- Refines Conditional Types [Aiken et al. '94]



<□ > < @ > < E > < E > E のQ @







• Type of a variable is flow-invariant



- Type of a variable is flow-invariant
- Flow sensitivity:

- Type of a variable is flow-invariant
- Flow sensitivity:
  - Makes variable types less clear

- Type of a variable is flow-invariant
- Flow sensitivity:
  - Makes variable types less clear
  - Brittle to refactoring

- Type of a variable is flow-invariant
- Flow sensitivity:
  - Makes variable types less clear
  - Brittle to refactoring
  - Doesn't help that much

- Type of a variable is flow-invariant
- Flow sensitivity:
  - Makes variable types less clear
  - Brittle to refactoring
  - Doesn't help that much
- Could be added later if needed

#### $\star$ \* Asymmetric Concatenation \* $\star$

• In PL design, asymmetry can be good

### $\star$ \* Asymmetric Concatenation \* $\star$

• In PL design, asymmetry can be good

▲ロト ▲帰ト ▲ヨト ▲ヨト - ヨ - の々ぐ

• Examples of asymmetry:

• In PL design, asymmetry can be good

▲ロト ▲帰ト ▲ヨト ▲ヨト - ヨ - の々ぐ

- Examples of asymmetry:
  - Subtyping

• In PL design, asymmetry can be good

▲ロト ▲帰ト ▲ヨト ▲ヨト - ヨ - の々ぐ

- Examples of asymmetry:
  - Subtyping
  - Overriding

• In PL design, asymmetry can be good

- Examples of asymmetry:
  - Subtyping
  - Overriding
  - Multiple inheritance

• In PL design, asymmetry can be good

- Examples of asymmetry:
  - Subtyping
  - Overriding
  - Multiple inheritance
  - Evaluation order

• In PL design, asymmetry can be good

- Examples of asymmetry:
  - Subtyping
  - Overriding
  - Multiple inheritance
  - Evaluation order
  - Module dependencies

### **\star** \* Asymmetric Concatenation \* **\star**

• Onion projection prefers rightmost element

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへぐ

• Onion projection prefers rightmost element

• Not based on row typing

- Onion projection prefers rightmost element
- Not based on row typing
- Only presence information is pushed forward

- Onion projection prefers rightmost element
- Not based on row typing
- Only presence information is pushed forward
  - Type system can express " $\alpha$  has 'A int"

- Onion projection prefers rightmost element
- Not based on row typing
- Only presence information is pushed forward
  - Type system can express " $\alpha$  has 'A int"

• But not " $\alpha$  only has 'A int"

- Onion projection prefers rightmost element
- Not based on row typing
- Only presence information is pushed forward
  - Type system can express " $\alpha$  has 'A int"

- But not " $\alpha$  only has 'A int"
- Upper bounds inferred from usage

- Onion projection prefers rightmost element
- Not based on row typing
- Only presence information is pushed forward
  - Type system can express " $\alpha$  has 'A int"
  - But not "α only has 'A int"
- Upper bounds inferred from usage
- Monomorphic variant of TinyBang closure is polynomial (vs. previous NP-complete result [Palsberg et al. '03])

• For scripts, edit-compile-debug must be fast

▲□▶ ▲圖▶ ★ 国▶ ★ 国▶ - 国 - のへで

• For scripts, edit-compile-debug must be fast

• Type constraint closure can be slow

• For scripts, edit-compile-debug must be fast

- Type constraint closure can be slow
- Solution:

- For scripts, edit-compile-debug must be fast
- Type constraint closure can be slow
- Solution:
  - Track differences between software versions

- For scripts, edit-compile-debug must be fast
- Type constraint closure can be slow
- Solution:
  - Track differences between software versions

• Delete constraints for removed code

- For scripts, edit-compile-debug must be fast
- Type constraint closure can be slow
- Solution:
  - Track differences between software versions

- Delete constraints for removed code
- Include constraints from new code

- For scripts, edit-compile-debug must be fast
- Type constraint closure can be slow
- Solution:
  - Track differences between software versions

- Delete constraints for removed code
- Include constraints from new code
- Perform closure again

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 の�?

• Typical type system limitations

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへぐ

- Typical type system limitations
  - Recursion limits contour creation

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへぐ

- Typical type system limitations
  - Recursion limits contour creation
  - Flow-insensitivity

- Typical type system limitations
  - Recursion limits contour creation
  - Flow-insensitivity
- Syntactic limitations

- Typical type system limitations
  - Recursion limits contour creation
  - Flow-insensitivity
- Syntactic limitations
  - No string-to-label functionality

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 の�?

What will we want out of a compiler?

• Compiles scripts to native binaries (via LLVM)

▲ロト ▲帰ト ▲ヨト ▲ヨト 三日 - の々ぐ

What will we want out of a compiler?

• Compiles scripts to native binaries (via LLVM)

• Optimizes layout using type information

What will we want out of a compiler?

• Compiles scripts to native binaries (via LLVM)

- Optimizes layout using type information
  - No unnecessary boxing

What will we want out of a compiler?

• Compiles scripts to native binaries (via LLVM)

- Optimizes layout using type information
  - No unnecessary boxing
  - Reduce pointer arithmetic

What will we want out of a compiler?

• Compiles scripts to native binaries (via LLVM)

- Optimizes layout using type information
  - No unnecessary boxing
  - Reduce pointer arithmetic
  - Definitely no runtime hashing

What will we want out of a compiler?

• Compiles scripts to native binaries (via LLVM)

- Optimizes layout using type information
  - No unnecessary boxing
  - Reduce pointer arithmetic
  - Definitely <u>no</u> runtime hashing
- Still path-sensitive across modules

What will we want out of a compiler?

• Compiles scripts to native binaries (via LLVM)

- Optimizes layout using type information
  - No unnecessary boxing
  - Reduce pointer arithmetic
  - Definitely <u>no</u> runtime hashing
- Still path-sensitive across modules

How do we get this?

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへぐ

Why do we need a whole-program view?

• No declarations of types or module signatures

Why do we need a whole-program view?

- No declarations of types or module signatures
- General layout for extensible data structures is inefficient

Why do we need a whole-program view?

- No declarations of types or module signatures
- General layout for extensible data structures is inefficient
- So we must know what could arrive at each call site

How can we live with ourselves?

 Intermediate work (constraint sets, etc.) can be stored and reused

How can we live with ourselves?

- Intermediate work (constraint sets, etc.) can be stored and reused
- Coding to a module signature is limited; not all interface semantics are typeable

How can we live with ourselves?

- Intermediate work (constraint sets, etc.) can be stored and reused
- Coding to a module signature is limited; not all interface semantics are typeable

• Vast layout optimization potential

How can we live with ourselves?

- Intermediate work (constraint sets, etc.) can be stored and reused
- Coding to a module signature is limited; not all interface semantics are typeable

- Vast layout optimization potential
- Shared libraries are still possible



- Standard approach: common layout form (as C++)





- Standard approach: common layout form (as C++)
- Existing work handles flexible data structures

◆□▶ ◆□▶ ◆三▶ ◆三▶ 三三 のへぐ

- Standard approach: common layout form (as C++)
- Existing work handles flexible data structures
  - A Calculus with Polymorphic and Polyvariant Flow Types [Wells et al. '02]

- Standard approach: common layout form (as C++)
- Existing work handles flexible data structures
  - A Calculus with Polymorphic and Polyvariant Flow Types [Wells et al. '02]

• A Polymorphic Record Calculus and Its Compilation [Ohori '95]

- Standard approach: common layout form (as C++)
- Existing work handles flexible data structures
  - A Calculus with Polymorphic and Polyvariant Flow Types [Wells et al. '02]

- A Polymorphic Record Calculus and Its Compilation [Ohori '95]
- Onions: more flexible, new problems

- Standard approach: common layout form (as C++)
- Existing work handles flexible data structures
  - A Calculus with Polymorphic and Polyvariant Flow Types [Wells et al. '02]

- A Polymorphic Record Calculus and Its Compilation [Ohori '95]
- Onions: more flexible, new problems
- Whole-program types will help us!

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 の�?

We have:

• A TinyBang interpreter

We have:

- A TinyBang interpreter
- A TinyBang type system and soundness proof

▲ロト ▲帰ト ▲ヨト ▲ヨト 三日 - の々ぐ

We have:

- A TinyBang interpreter
- A TinyBang type system and soundness proof

• Effective encodings for language features

We have:

- A TinyBang interpreter
- A TinyBang type system and soundness proof

• Effective encodings for language features

We need:

We have:

- A TinyBang interpreter
- A TinyBang type system and soundness proof

• Effective encodings for language features

We need:

• A TinyBang-to-LLVM compiler

We have:

- A TinyBang interpreter
- A TinyBang type system and soundness proof

• Effective encodings for language features

We need:

- A TinyBang-to-LLVM compiler
- A BigBang metaprogramming system

We have:

- A TinyBang interpreter
- A TinyBang type system and soundness proof
- Effective encodings for language features

We need:

- A TinyBang-to-LLVM compiler
- A BigBang metaprogramming system
- A layout calculus and optimization tool

We have:

- A TinyBang interpreter
- A TinyBang type system and soundness proof
- Effective encodings for language features

We need:

- A TinyBang-to-LLVM compiler
- A BigBang metaprogramming system
- A layout calculus and optimization tool

# Questions?

◆□▶ ◆□▶ ◆臣▶ ◆臣▶ 臣 のへぐ